Geometry of Random Stepped Surfaces

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A stepped surface is a surface composed of squares from the cubic lattice, and which projects monotonically in the (1,1,1) direction. We study random stepped surfaces (with fixed boundary) and their limits when the lattice spacing tends to zero. Despite quite complicated formulas for the limit shapes (involving dilogarithms), there is a clean geometric formulation.